

# Estimating the source-location accuracy in the geothermal site of Los Humeros (Mexico) using sensitivity maps for time-reverse imaging

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# Why Time-Reverse Imaging (TRI)?



full waveform  
no picking → quasi-simultaneous & low signal-to-noise ratio events  
all scales (lab, field, ...) → non-destructive testing, **micro-seismic events**, tremors, ...



velocity model  
computational cost  
unknown constraints on **station network** → **This study**

# The method of TRI

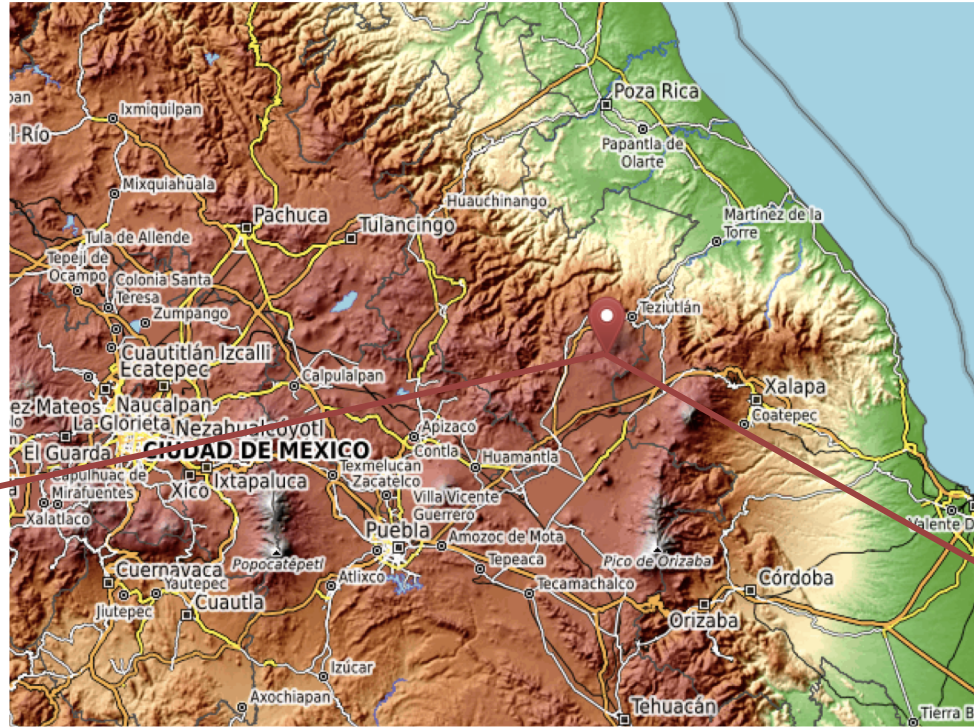
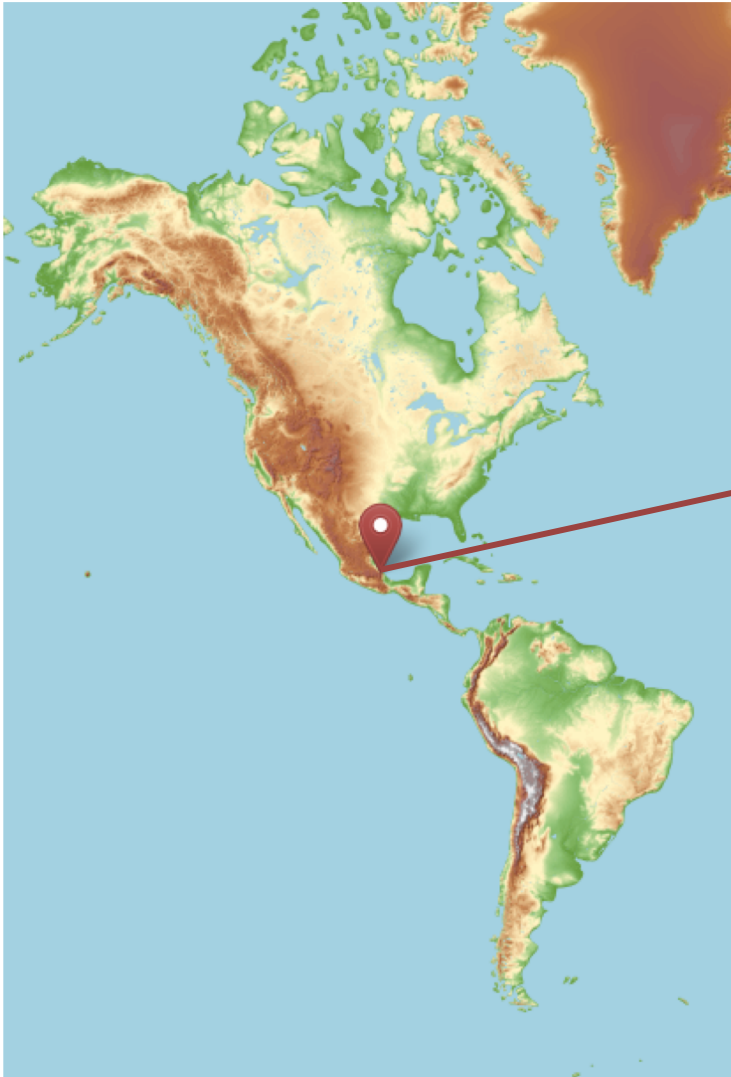
recorded at seismic stations



time-reversed traces



# Los Humeros geothermal field



part of Trans-Mexican Volcanic Belt  
multi-caldera structure  
superhot geothermal system



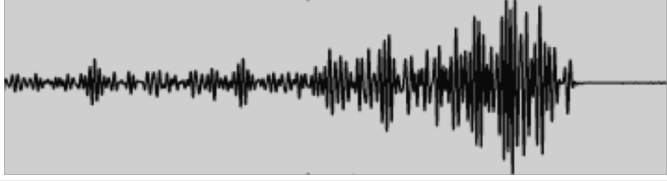


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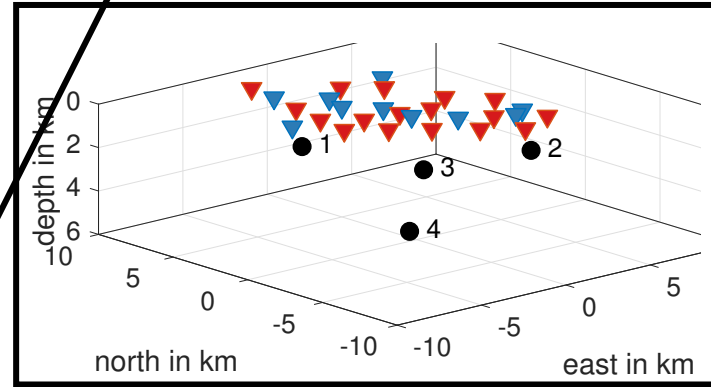
recorded at seismic stations



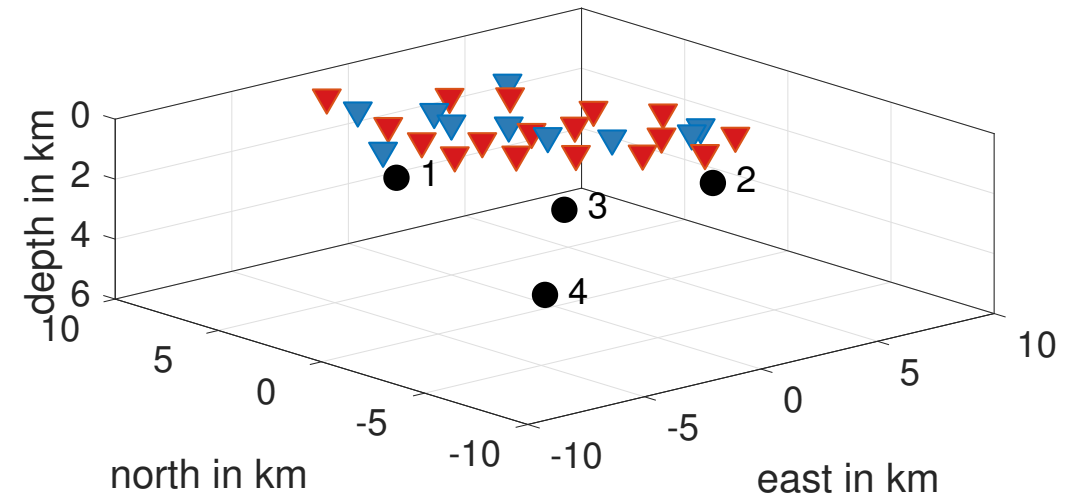
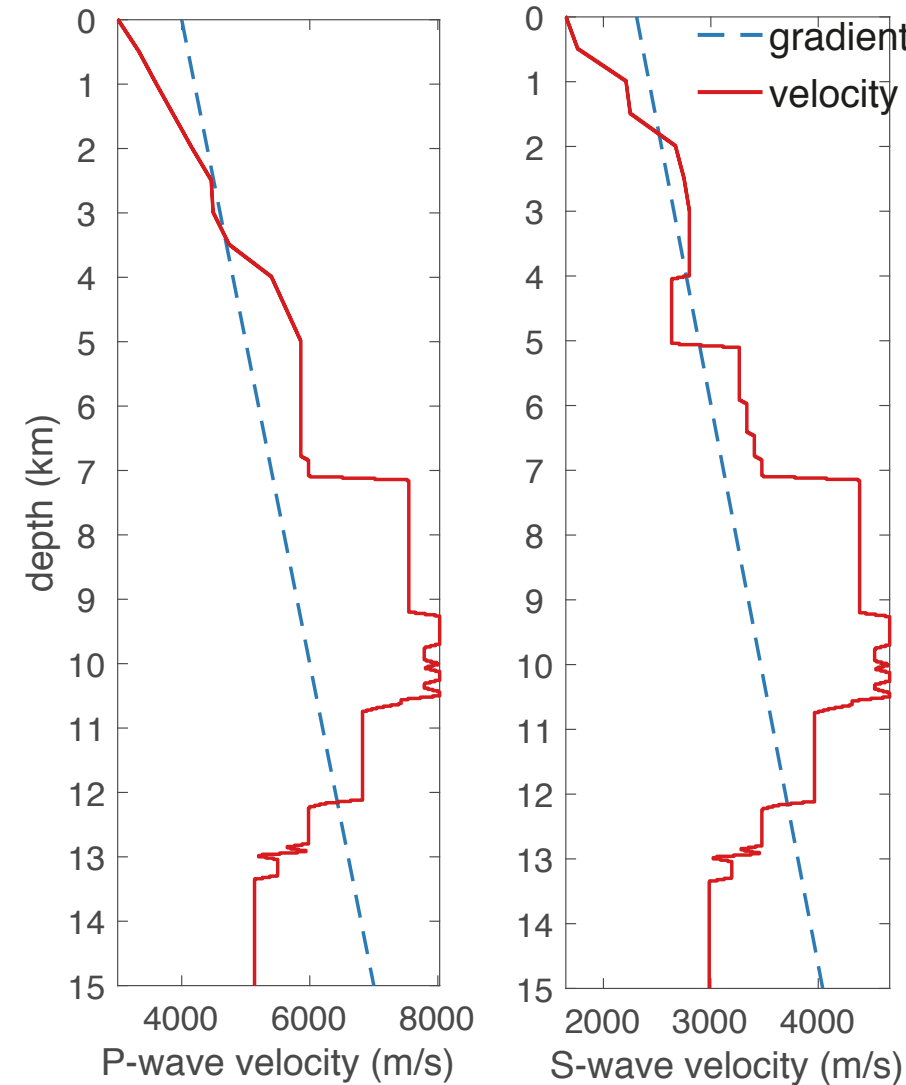
time-reversed traces



back propagate



# Los Humeros geothermal field: model set-up



- ▼ short period stations
- ▼ broadband stations
- synthetic sources

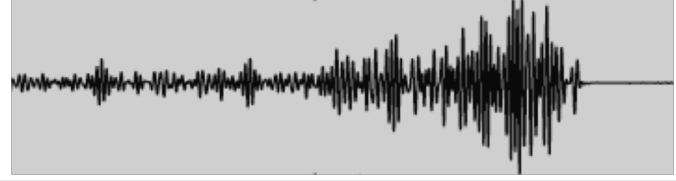
27 stations (deployed 09/2017 – 09/2018) and a 1D P- and S-wave velocity model are available

# The method of TRI

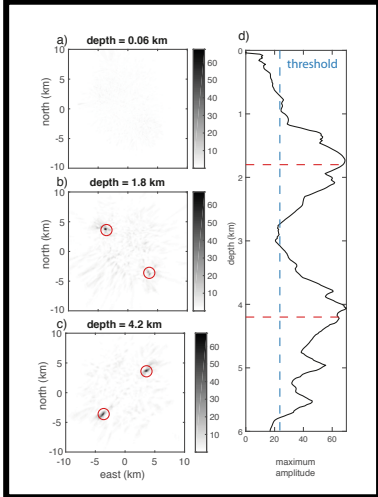
recorded at seismic stations



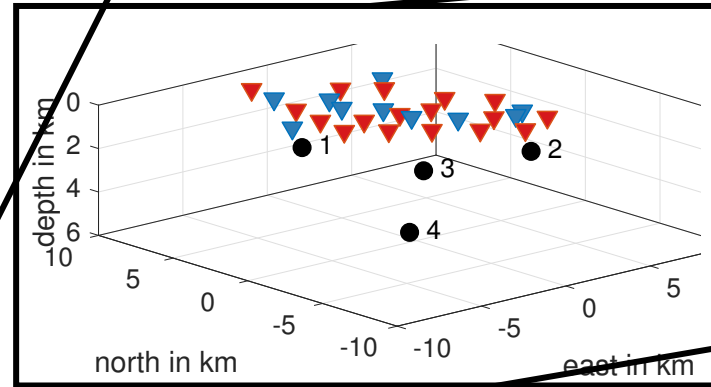
time-reversed traces



eliminate background noise



back propagate



imaging conditions

total energy density:

$$\mathbf{I}_e(\mathbf{x}) = \max_{t \in [0, T]} \sum_i \sum_j [\sigma_{ij}(\mathbf{x}, t) \varepsilon_{ij}(\mathbf{x}, t)]$$

P-wave energy density:

$$\mathbf{I}_p(\mathbf{x}) = \max_{t \in [0, T]} (\lambda + 2\mu) [\nabla \cdot \mathbf{u}(\mathbf{x}, t)]^2$$

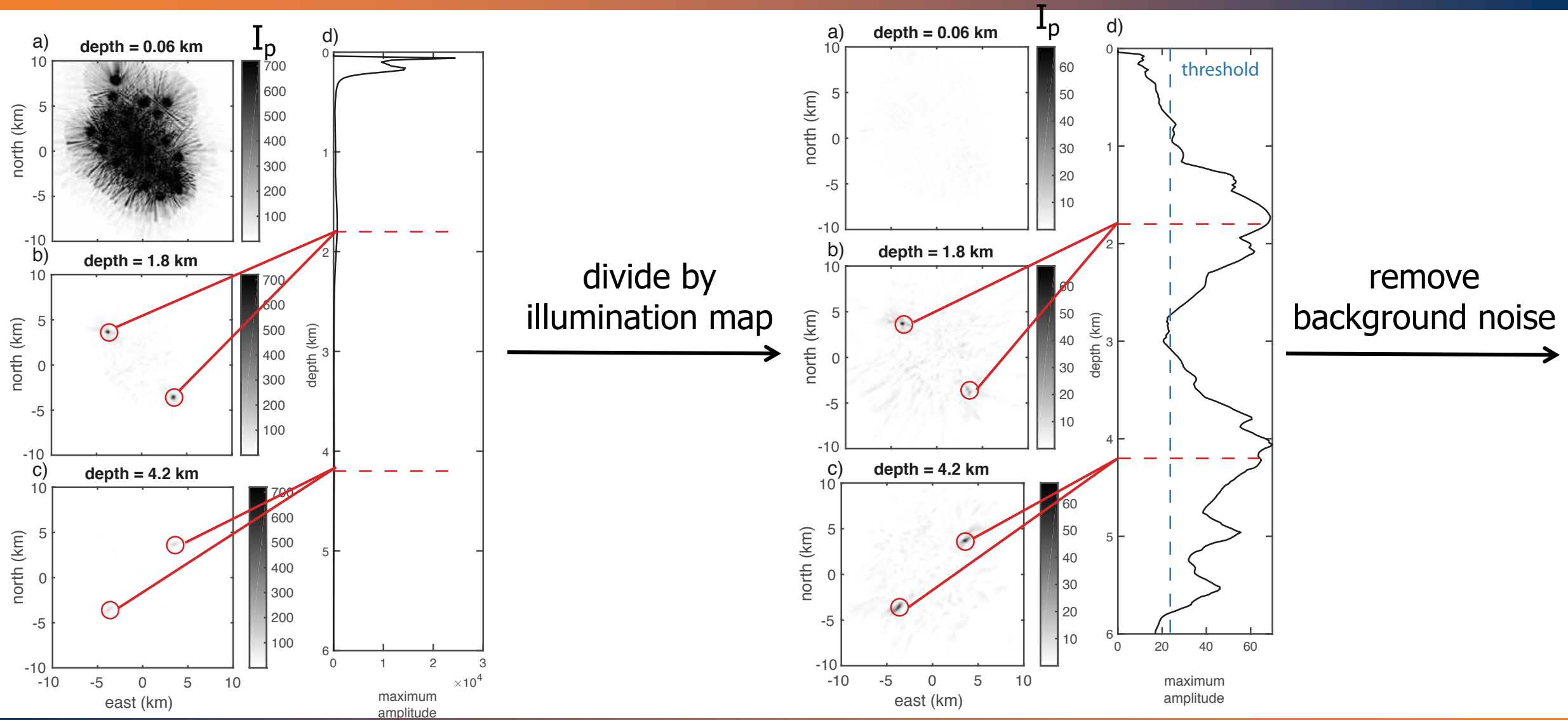
S-wave energy density:

$$\mathbf{I}_s(\mathbf{x}) = \max_{t \in [0, T]} \mu [\nabla \times \mathbf{u}(\mathbf{x}, t)]^2$$

$\mathbf{x}$ : space vector –  $t$ : time –  $\mathbf{u}$ : displacement –  
 $\lambda, \mu$ : Lamé parameters –  $\sigma_{ij}$ : stress –  $\varepsilon_{ij}$ : strain

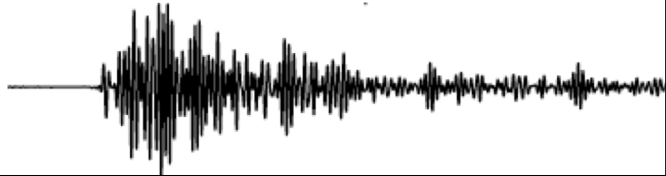
*Saenger (2011), NDT&E International*

# Removing artificial high amplitudes



# The method of TRI

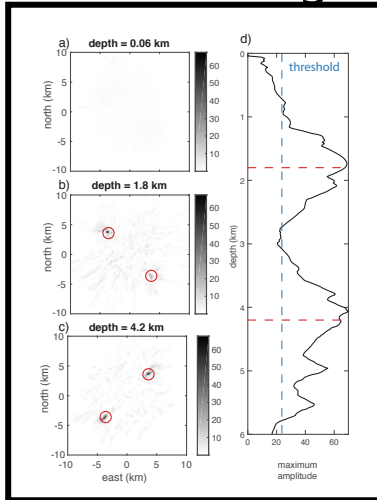
recorded at seismic stations



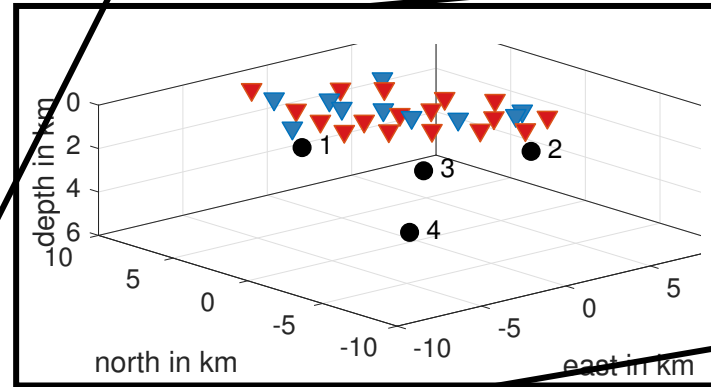
time-reversed traces



eliminate background noise



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imaging conditions

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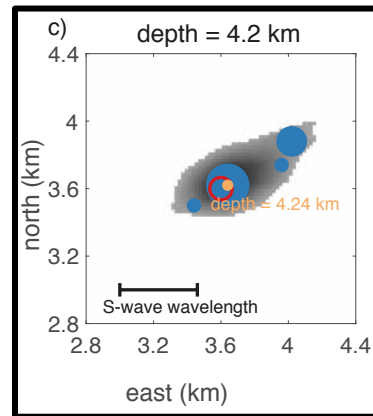
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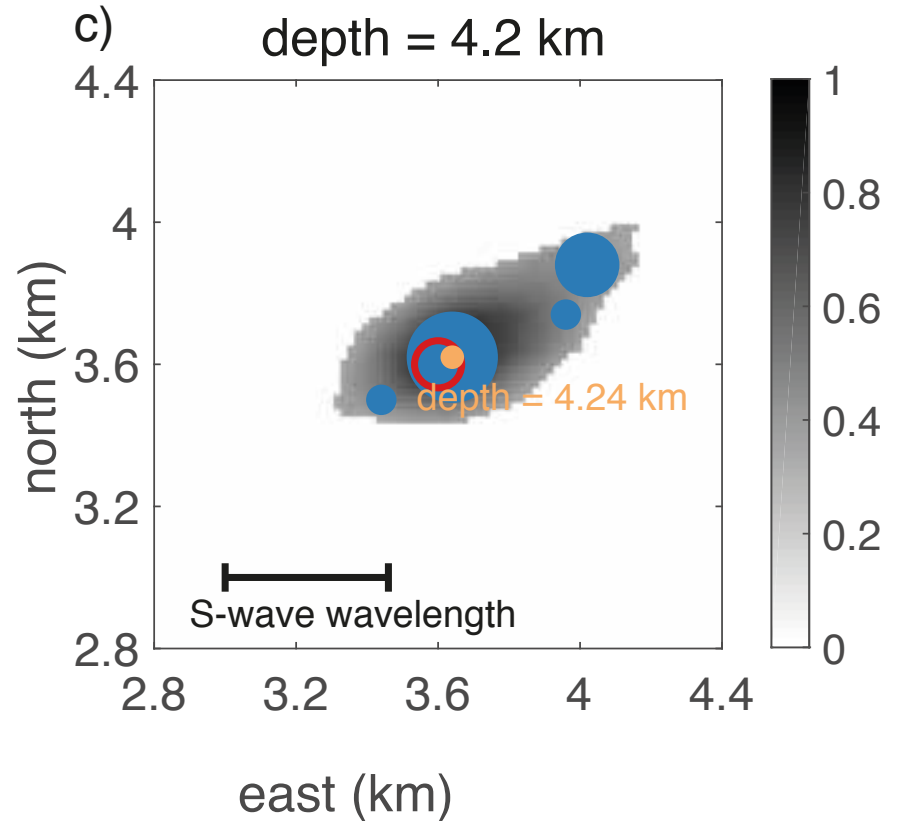
find source localisations



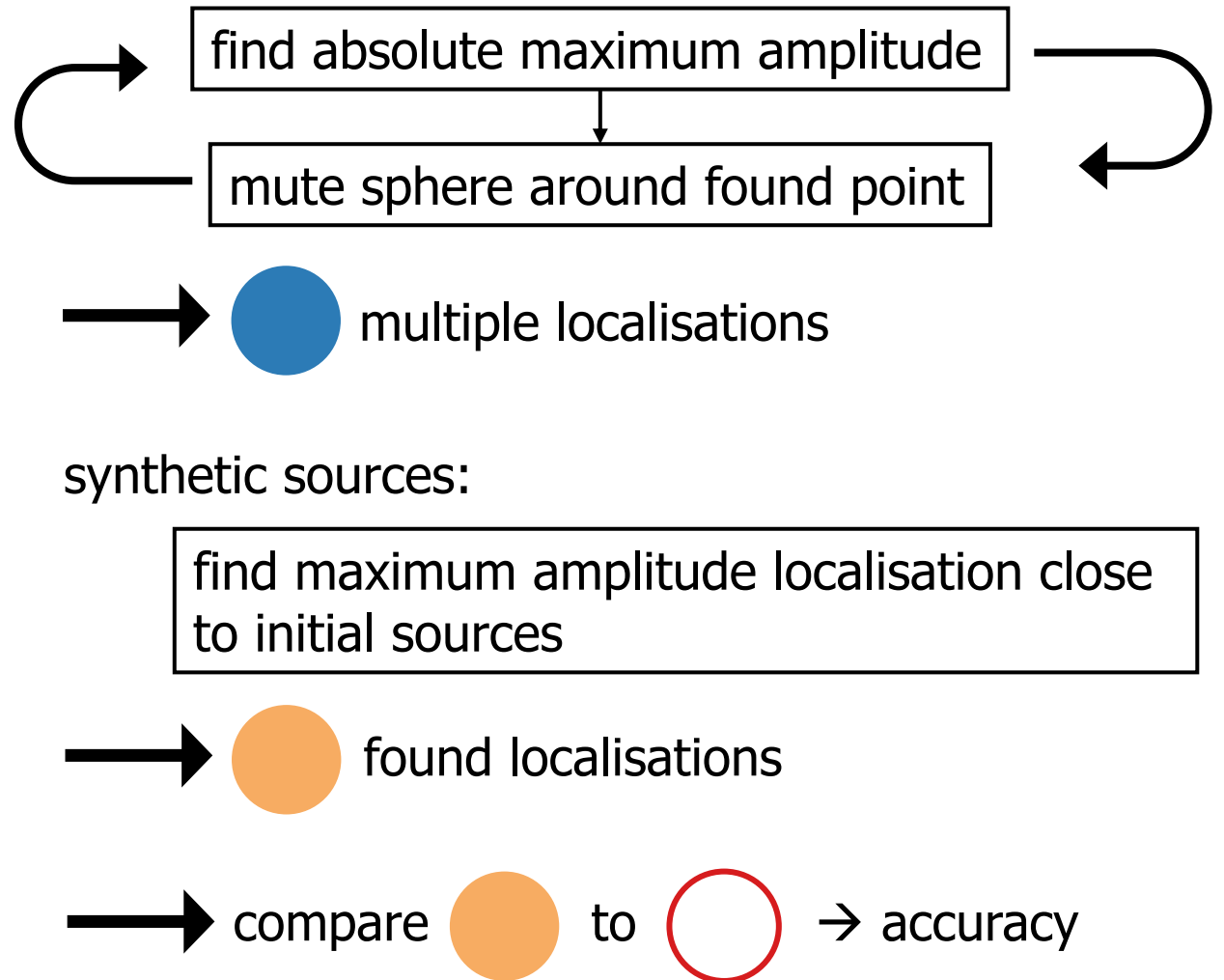
compare to initial sources



# Automatic identification of localisations

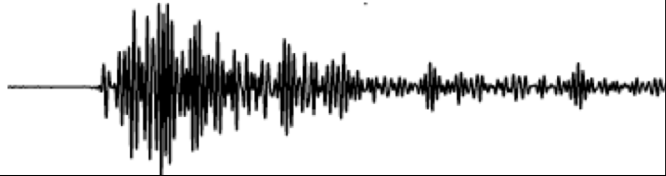


- found localisations (larger circles are closer to source depth)
- original source location
- identified source location



# The method of TRI

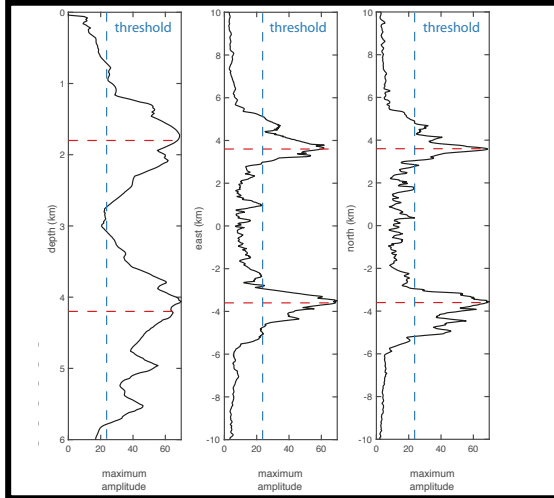
recorded at seismic stations



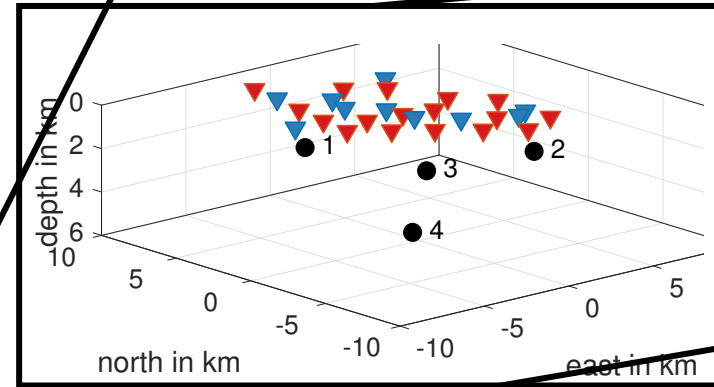
time-reversed traces



eliminate background noise



back propagate



imaging conditions

$$\text{total energy density:} \\ \mathbf{I}_e(\mathbf{x}) = \max_{t \in [0, T]} \sum_i \sum_j [\sigma_{ij}(\mathbf{x}, t) \varepsilon_{ij}(\mathbf{x}, t)]$$

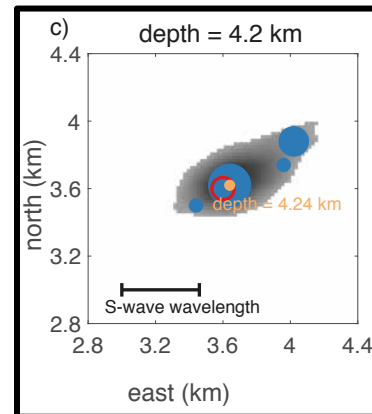
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find source localisations



compare to initial sources

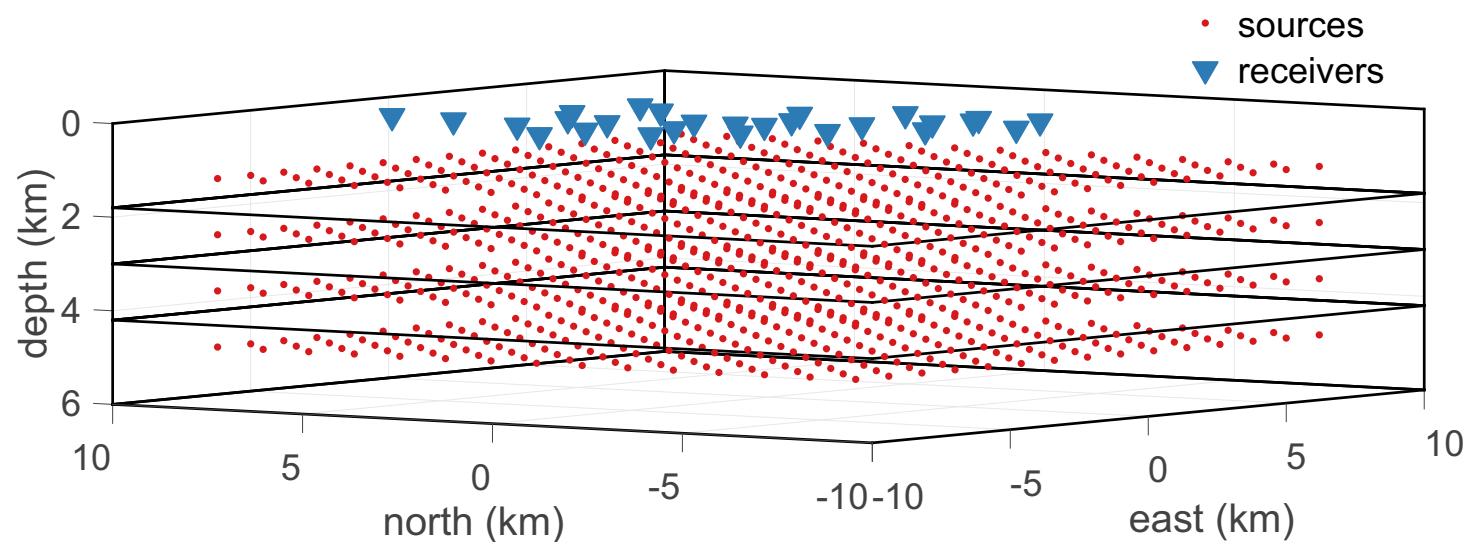
**Sensitivity Maps**

# How to create Sensitivity Maps

place numerous sources throughout the model following some guidelines:

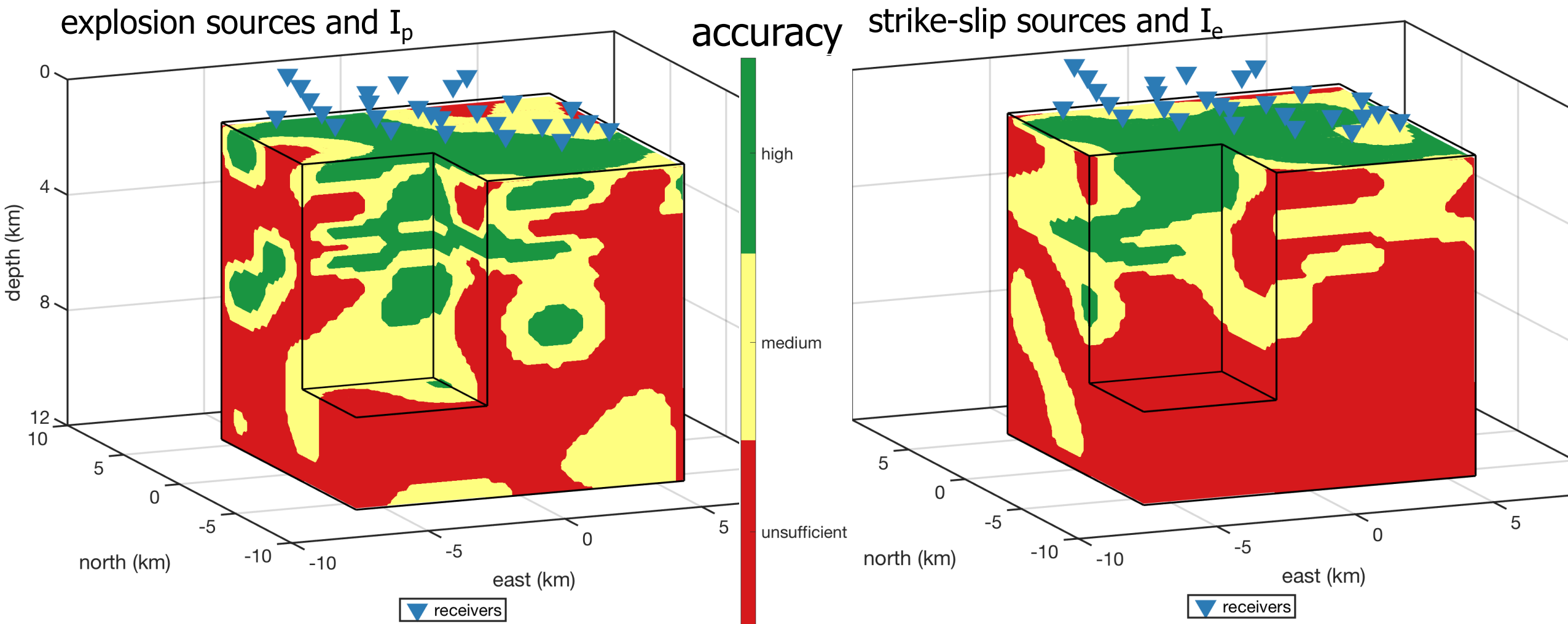
- 1) inter-source distance > maximum inter-station distance (here: > 2.1 km)
- 2) sources in only one depth per simulation
- 3) not too closer than 2 S-wave wavelengths to boundary

Then locate these sources with TRI and investigate the achieved spatial and temporal error.



A fast way to evaluate the location accuracy with a given station distribution and velocity model.

# Sensitivity Maps for the geothermal site Los Humeros

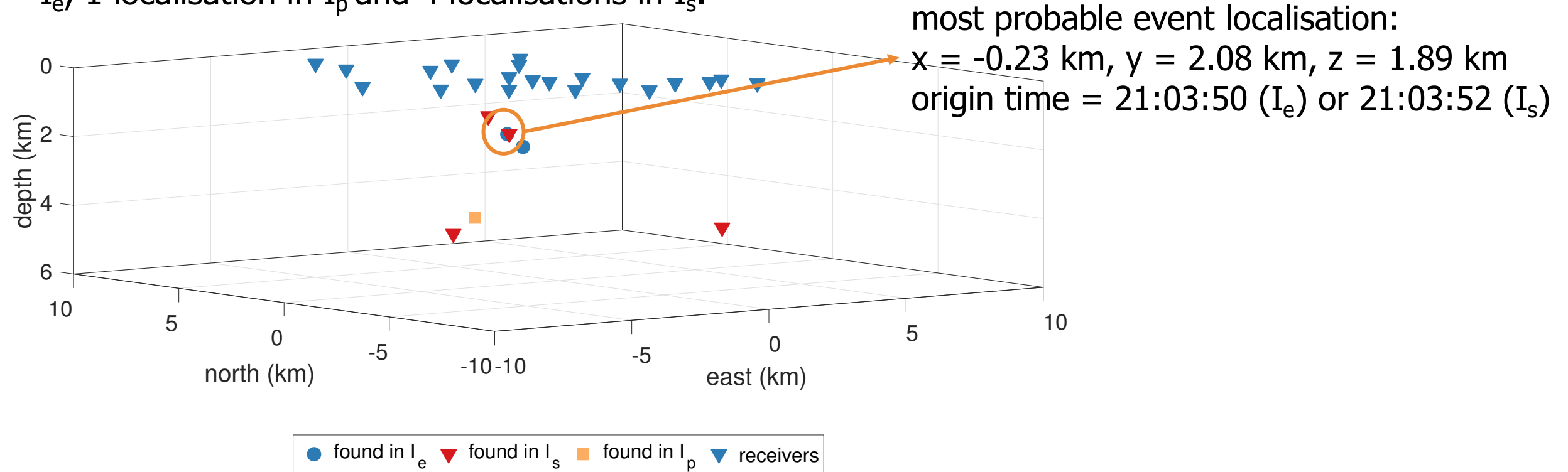


Accuracy is influenced by: station distribution, velocity model & source type.

# Located real-life micro-seismic event (magnitude $\sim 2.2$ )

recorded 2018/04/22 with 21 stations

After muting areas with insufficient accuracy and elimination of unrealistic localisations: 2 localisations in  $I_e$ , 1 localisation in  $I_p$  and 4 localisations in  $I_s$ .



Sensitivity Maps allow the localisation of real-life events



# Conclusions

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Work flow for the evaluation of source-location accuracy using TRI

## → **Sensitivity Maps** ←

### **work flow:**

user-independent  
low computational costs  
intuitive results

### **application:**

evaluate existing networks  
plan and optimise new networks  
enhance localisation of real-life events

### **next steps:**

Compare to localisations from other methods  
Identify source type

# Acknowledgements

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